

# Sensitivity Study of Persistent Contrail Development using Large Eddy Simulation

**Alexander D. Naiman and Sanjiva K. Lele**

*Department of Aeronautics and Astronautics*

**Mark Z. Jacobson**

*Department of Civil and Environmental Engineering*

*Stanford University*

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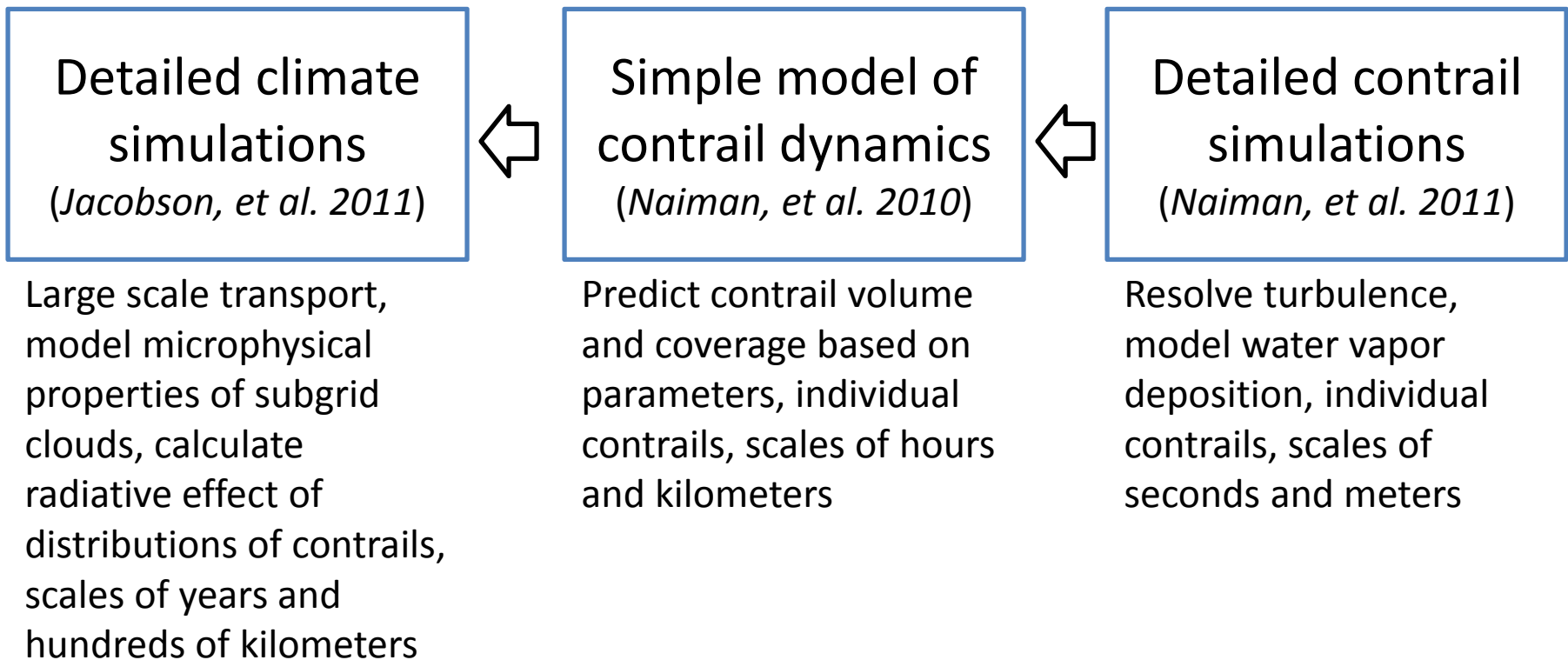
# Outline

- Project overview
- Description of simulations
- Sensitivity study results
- Comparison to parameterized contrail dynamics model
- Conclusions and future work



# Project Overview

Goal: Improve estimates of the climate impact of aviation through better understanding of physical processes



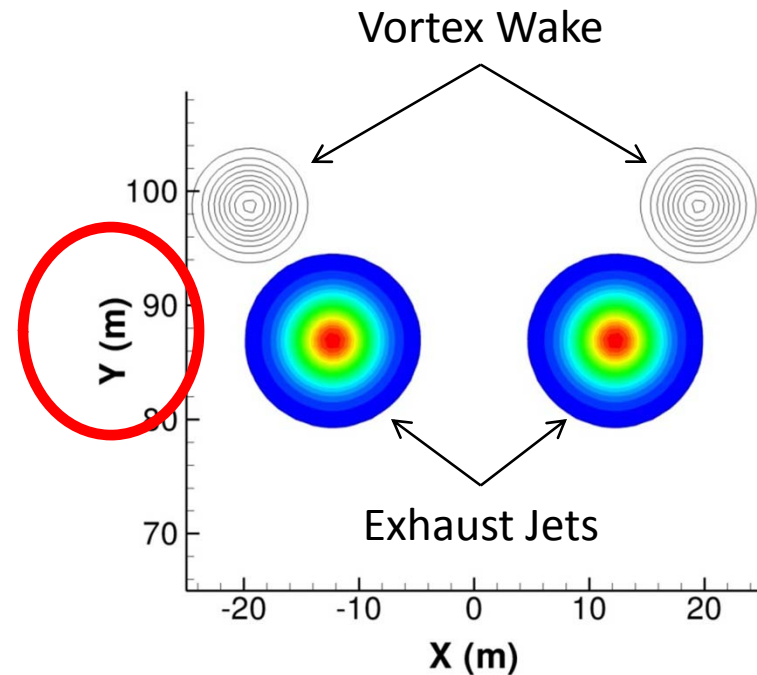
# Description of Simulations

- Incompressible 3D LES with Boussinesq approximation (*Mahesh, et al. 2004, Ham, et al. 2007*)
- Lagrangian ice particles with water deposition and sublimation
- Twenty minutes simulated from time of emission
- Sensitivity cases vary:
  - Aircraft type (3 cases)
  - Vertical wind shear (2 cases)
  - Ambient relative humidity (2 cases)
- Additional cases vary ice nuclei emission index and atmospheric stability, validation cases include inertial/sedimenting particles and resolution studies (not presented here)

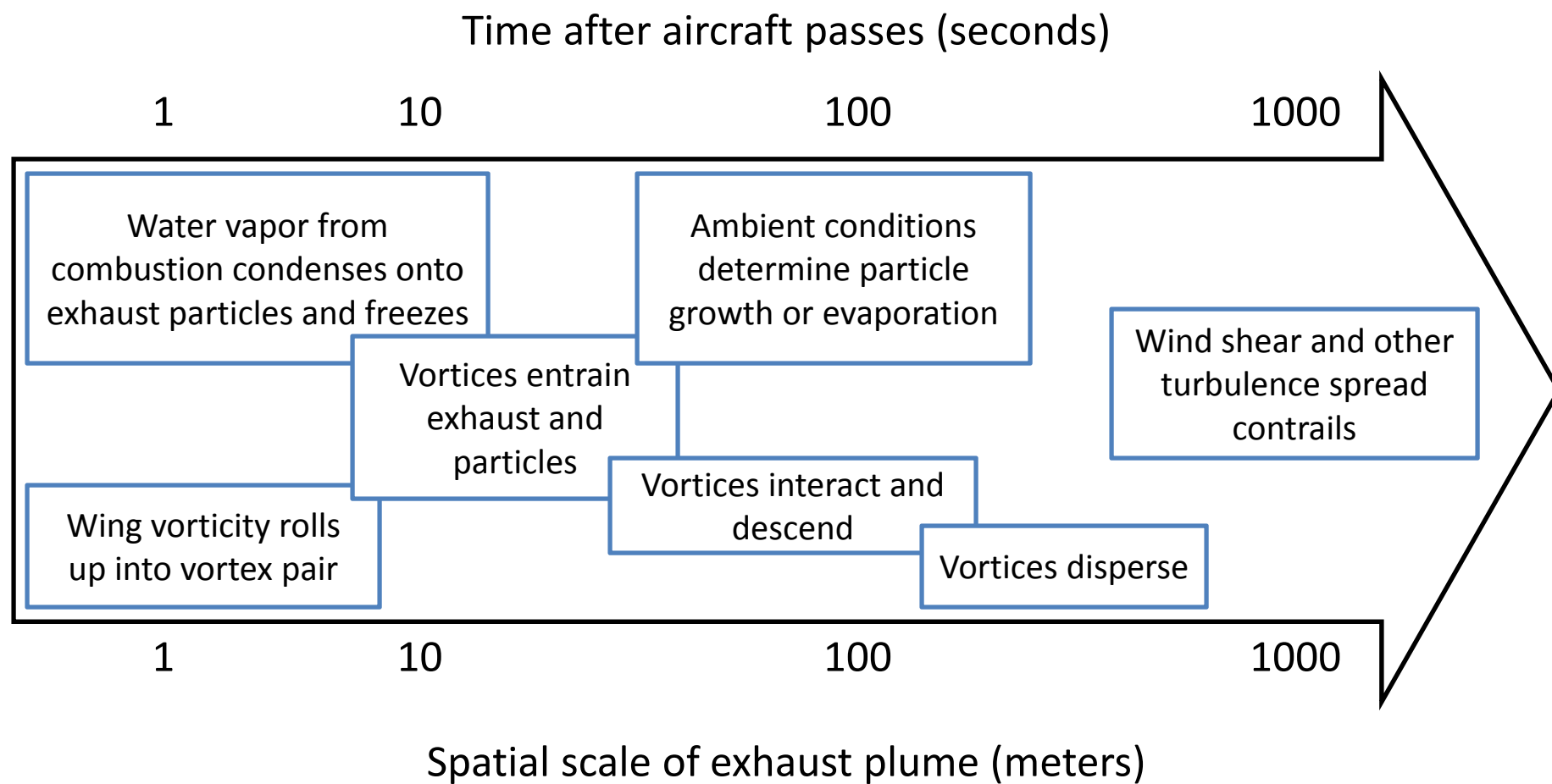


# Description of Simulations

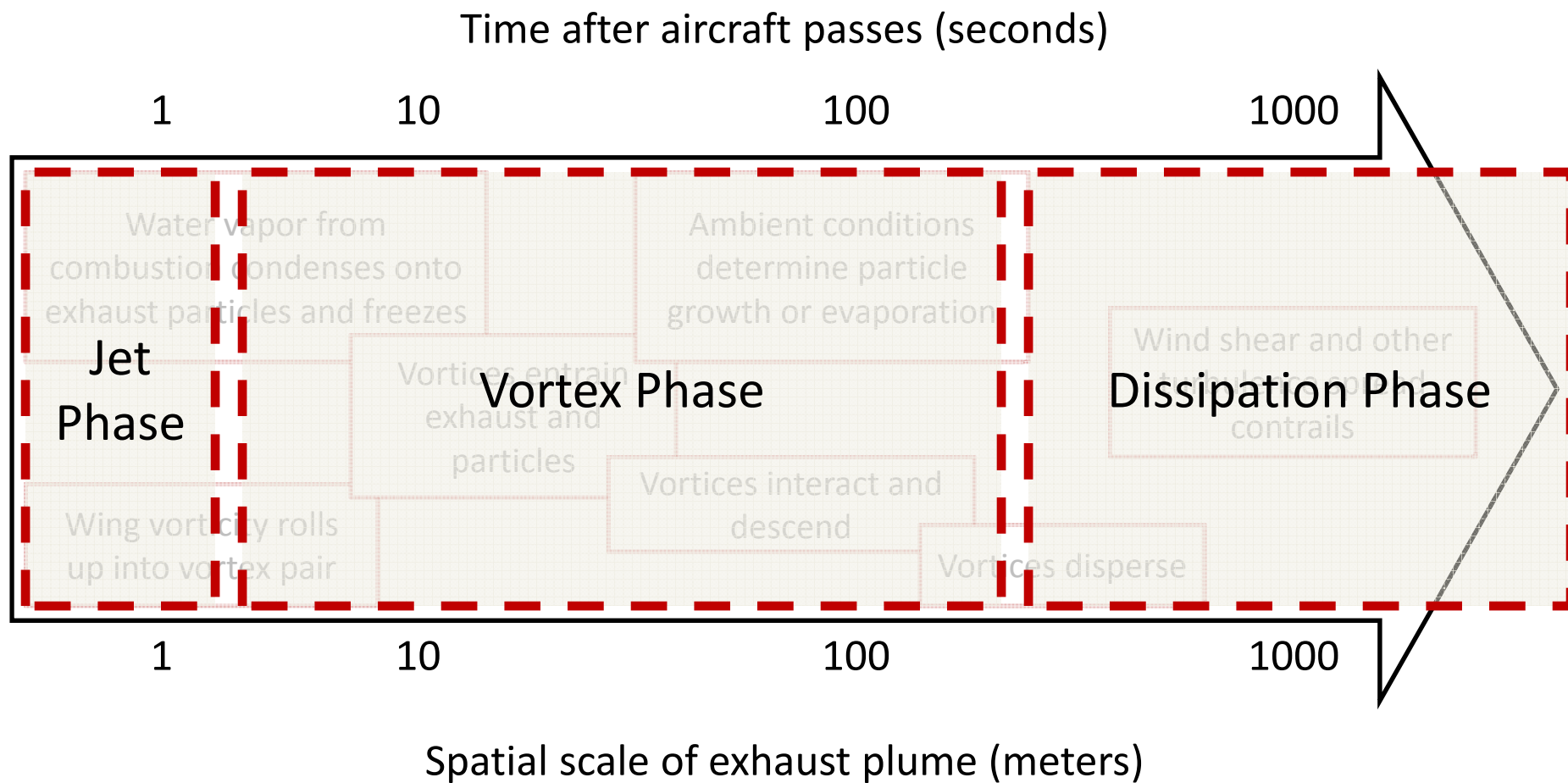
- Ambient conditions based on cruising commercial jet
  - 10.5 km altitude
  - Stable temperature gradient
  - Highly supersaturated w.r.t. ice to produce persistent contrails
- 3D Initial Condition uses idealized 2D vortex/jet field plus 3D decaying isotropic turbulence



# Description of Simulations

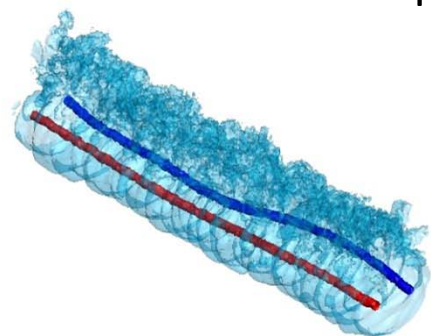


# Description of Simulations

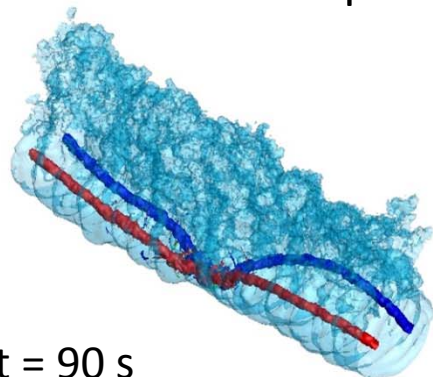


# Baseline Case – Crow Instability

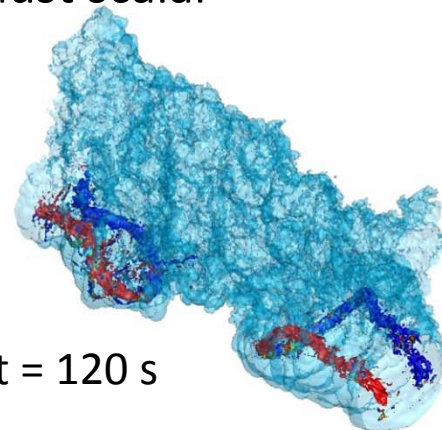
Isosurfaces of vorticity magnitude (colored by streamwise vorticity) inside transparent isosurfaces of the passive exhaust scalar



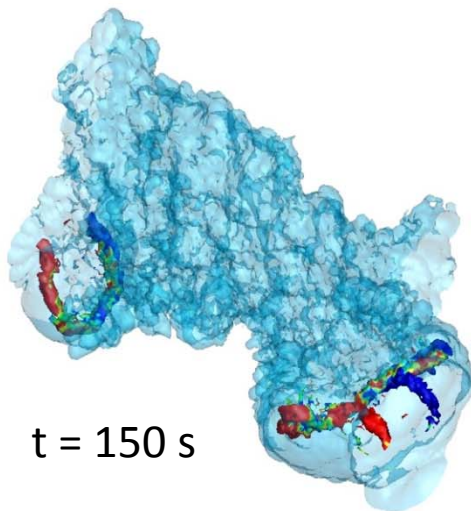
t = 65 s



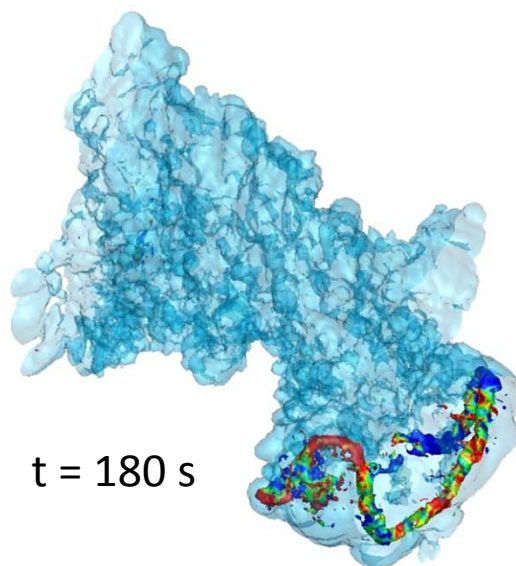
t = 90 s



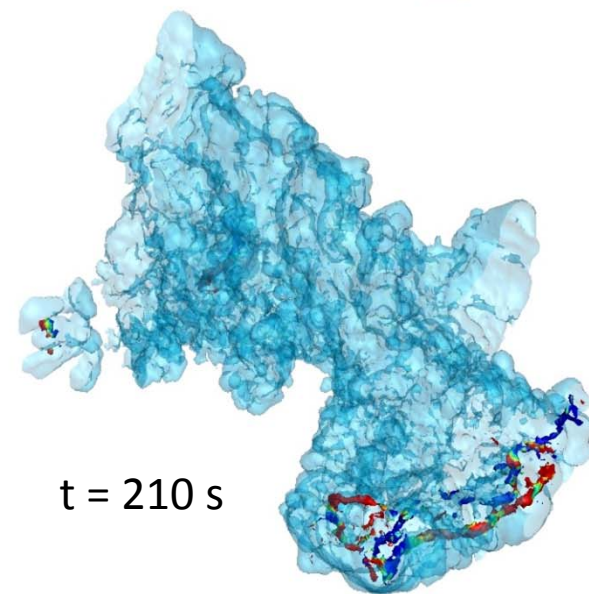
t = 120 s



t = 150 s



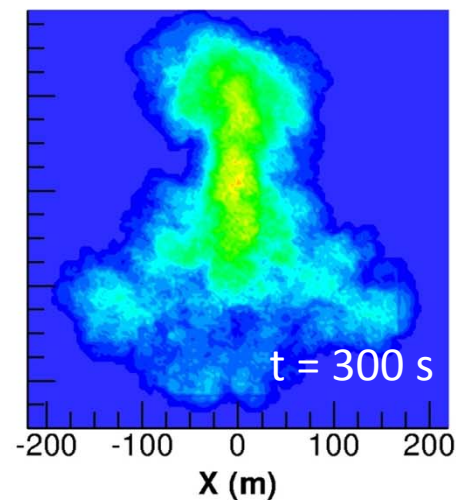
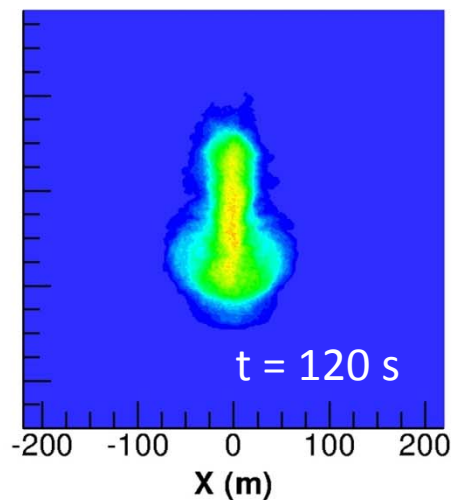
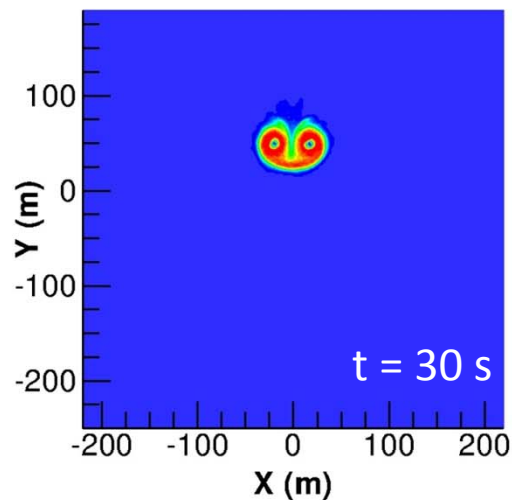
t = 180 s



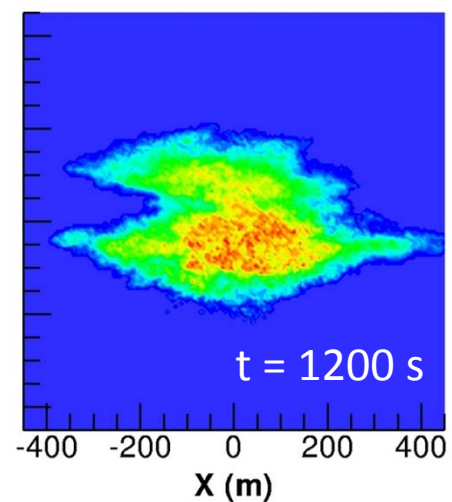
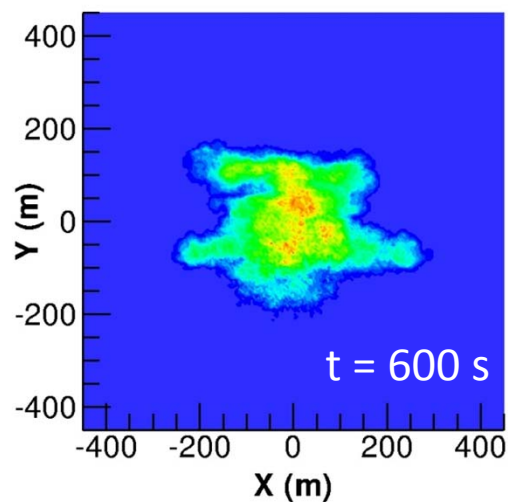
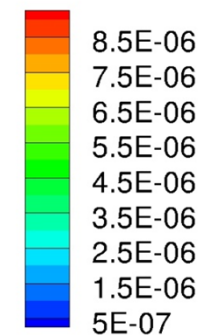
t = 210 s



# Baseline Case – Ice Density Contours

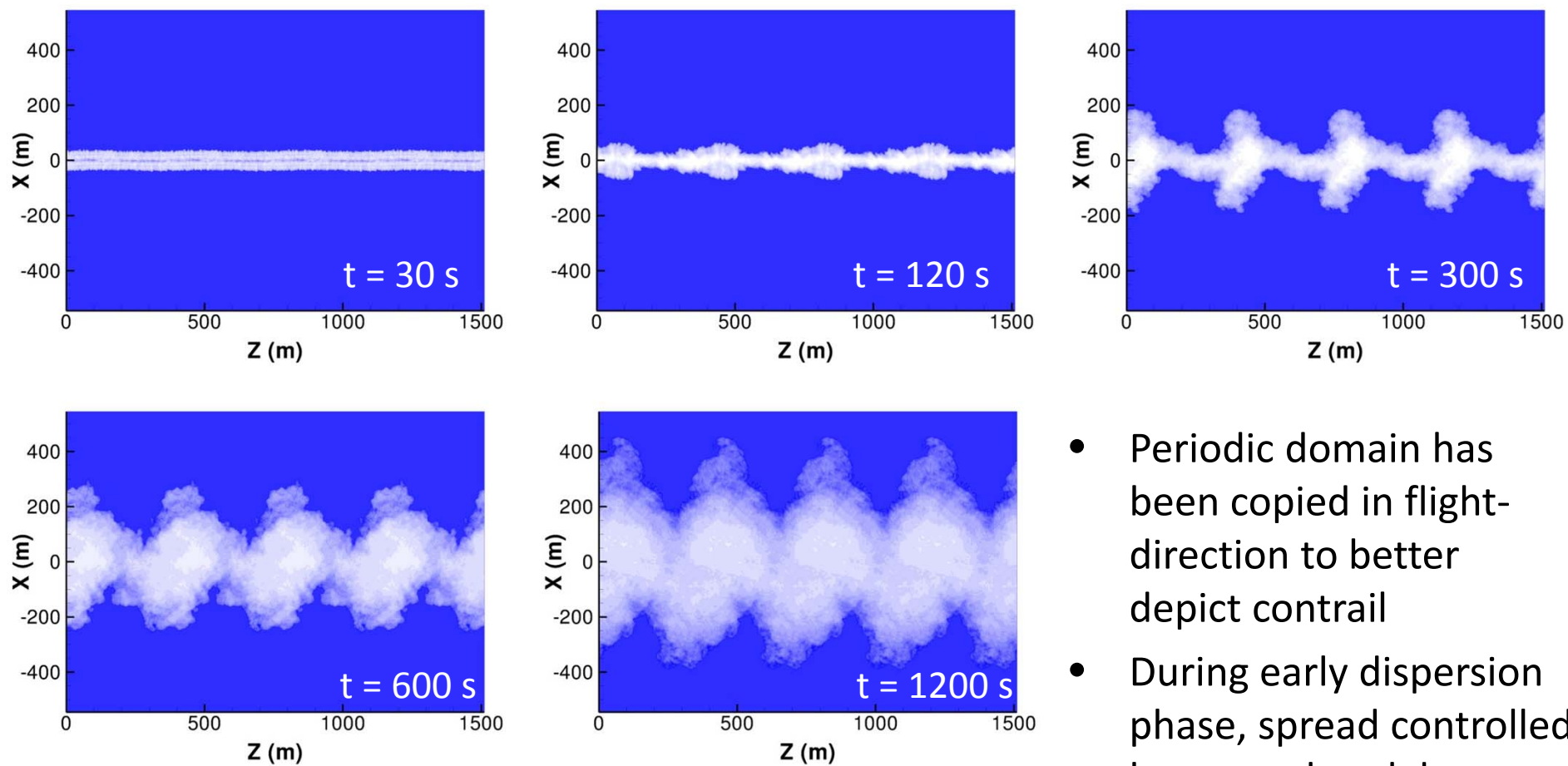


Ice Mass Density  
( $\text{kg/m}^3$ )

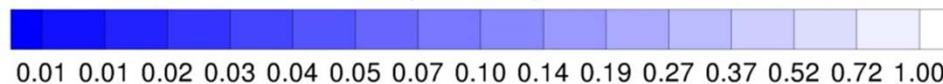


- Primary wake is spread horizontally after vortex breakdown
- Primary and secondary wake limited in vertical extent by stability

# Baseline Case – Optical Properties

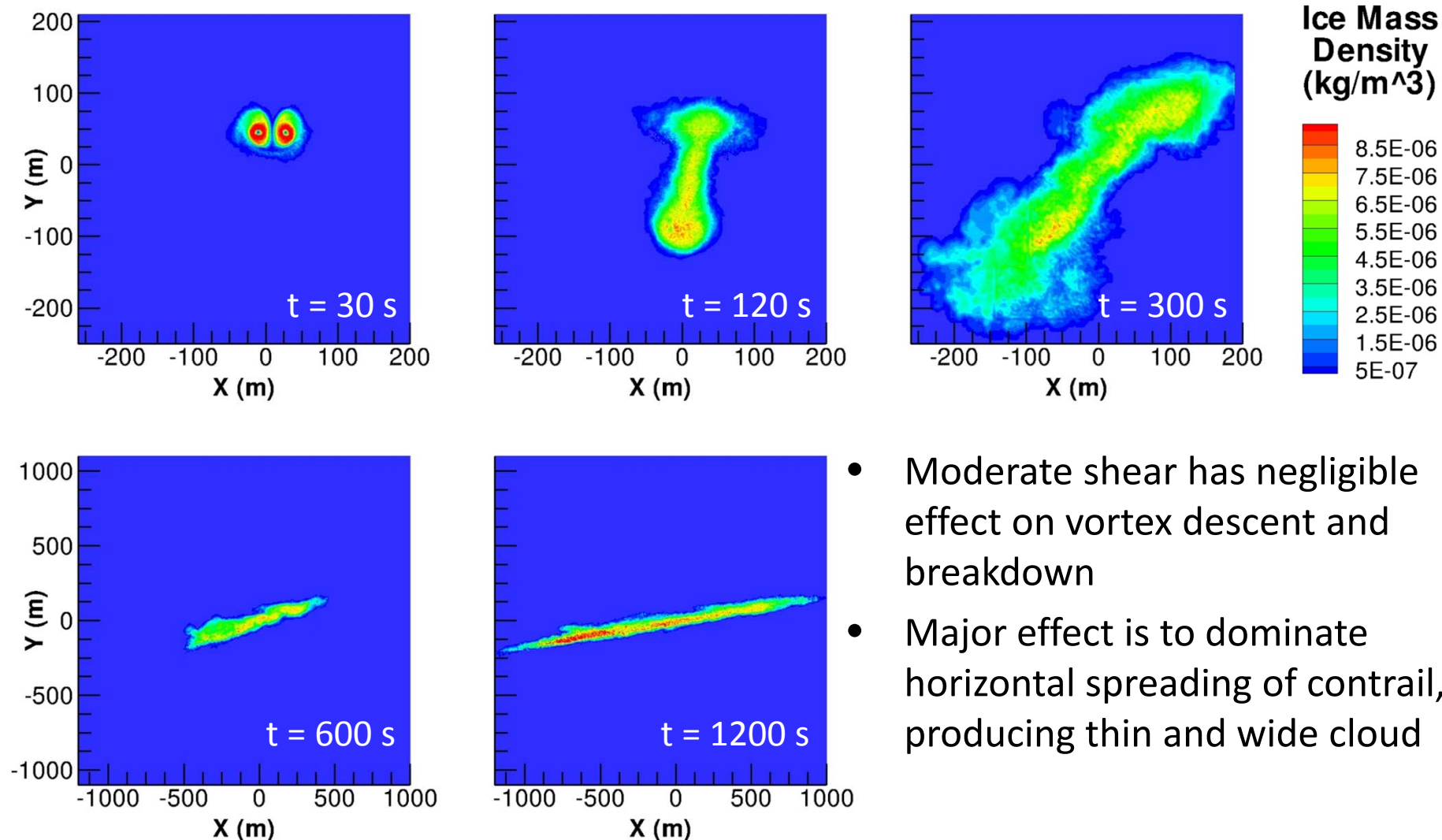


Optical Depth



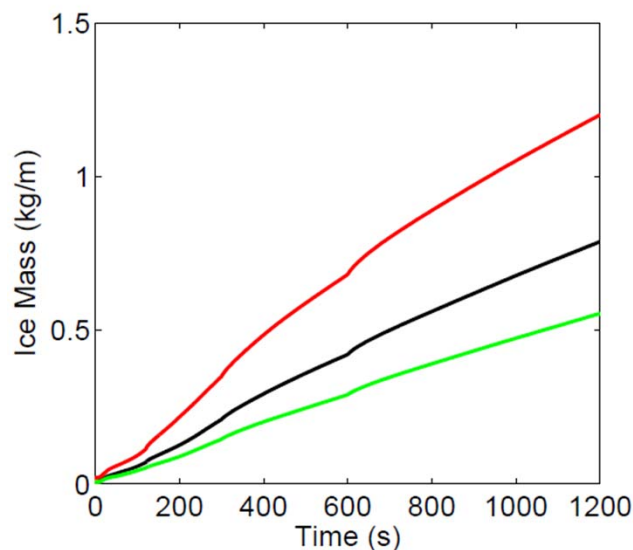
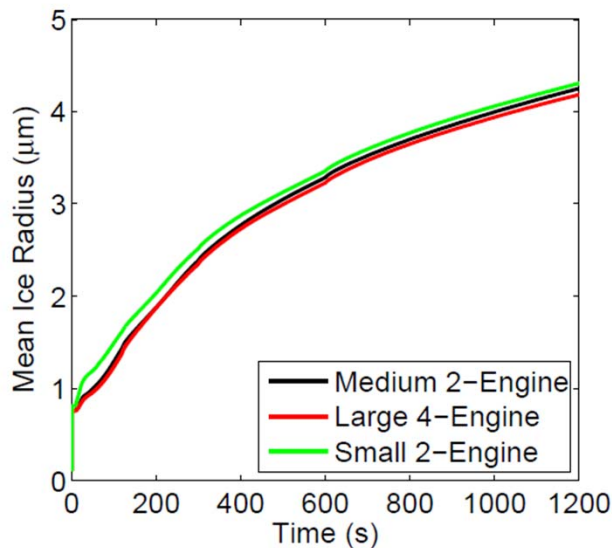
- Periodic domain has been copied in flight-direction to better depict contrail
- During early dispersion phase, spread controlled by vortex breakdown

# Shear Case – Ice Density Contours



- Moderate shear has negligible effect on vortex descent and breakdown
- Major effect is to dominate horizontal spreading of contrail, producing thin and wide cloud

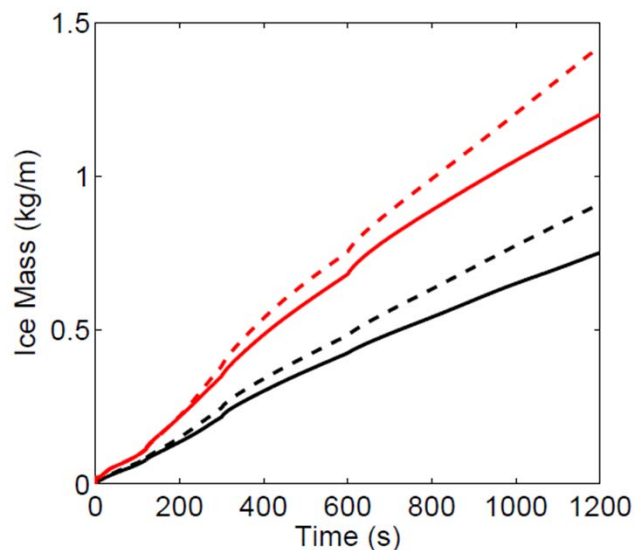
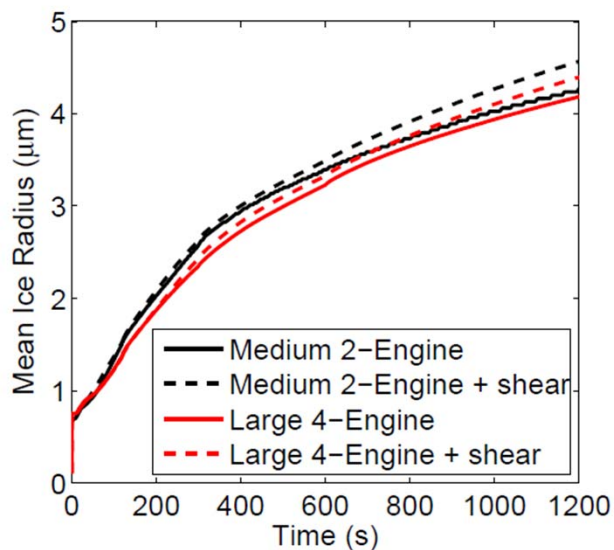
# Sensitivity Cases – Ice Statistics



- Aircraft type cases
  - Different initial conditions varied wing span, circulation strength, number of engines, and emissions (scaled by estimated fuel burn)
- Negligible differences in mean size of ice particles produced
- Integrated ice mass increased with aircraft size
  - Larger aircraft emit more ice nuclei and water vapor
  - Larger vortex wakes entrain more ambient water vapor

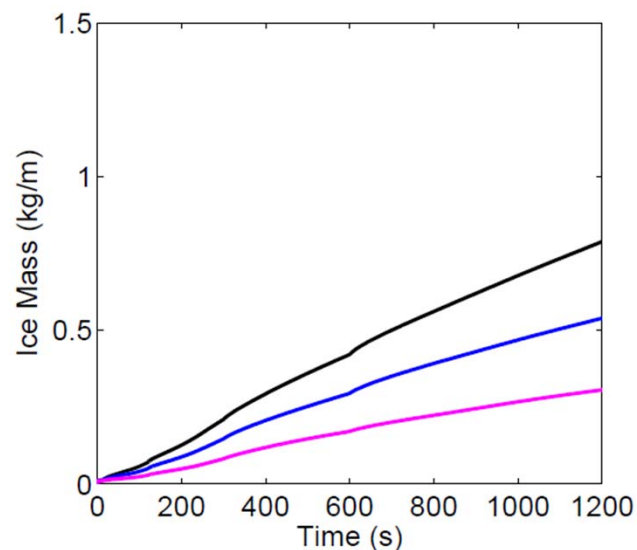
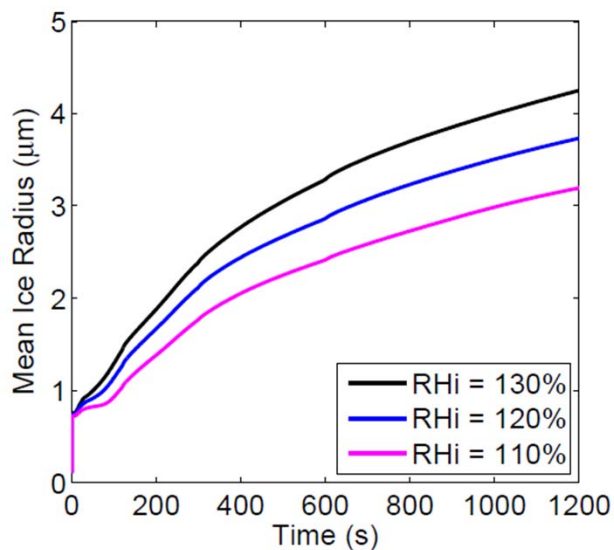


# Sensitivity Cases – Ice Statistics



- Vertical shear cases
  - Added moderate wind shear (5 m/s/km) to baseline medium and large aircraft cases
- Slight differences in mean size of ice particles produced
- Integrated ice mass increased with shear
  - Shear promotes entrainment of ambient air in dispersion phase
  - Increased mixing of humid air produces larger particles, more ice mass

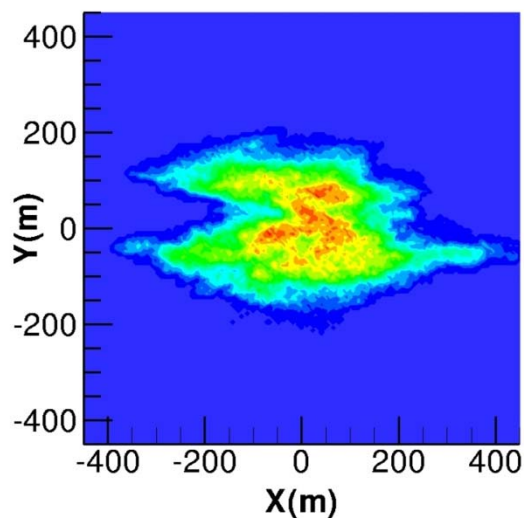
# Sensitivity Cases – Ice Statistics



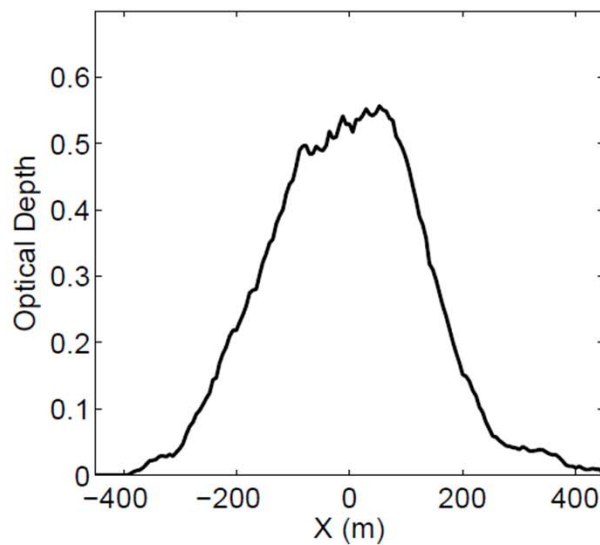
- Ambient relative humidity cases
  - Reduced RH<sub>i</sub> from baseline 130% medium aircraft case
- Higher humidity produced larger ice particles
- Integrated ice mass also increased with humidity
  - Entrainment of ambient water vapor controls ice growth in persistent contrails
  - Higher humidity cases provide more water vapor for deposition to ice



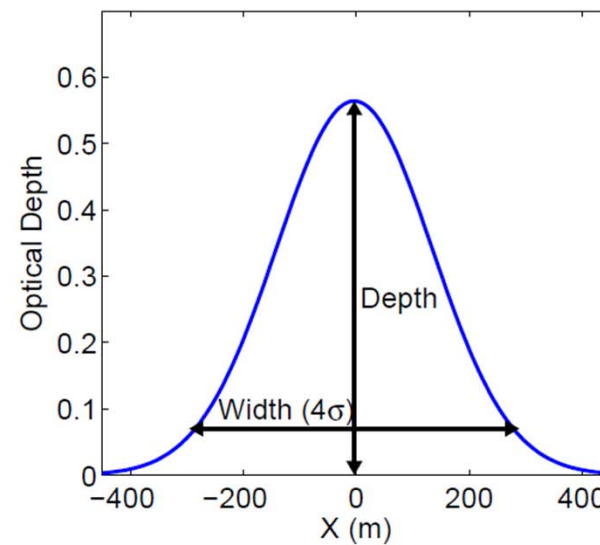
# Contrail Optical Calculations



Z-averaged optical  
extinction



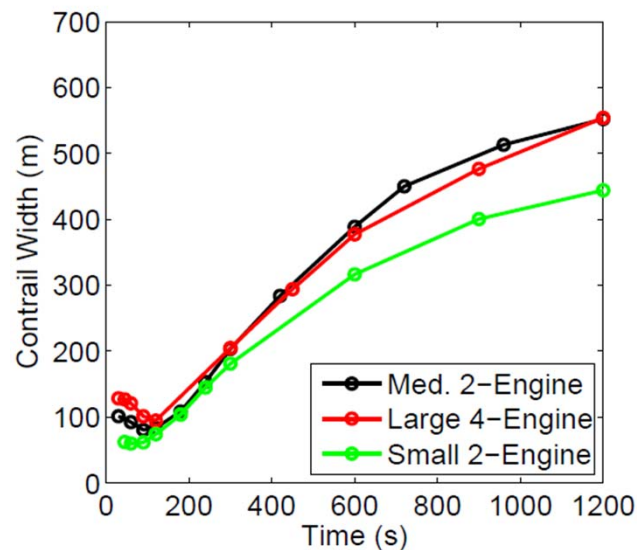
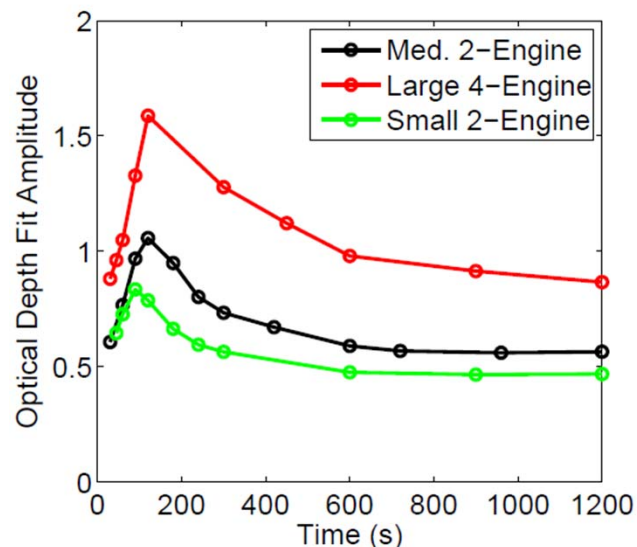
Optical depth



Gaussian fit

Contrail optical depth and width reported from fit of  
Gaussian to flight-direction averaged optical depth

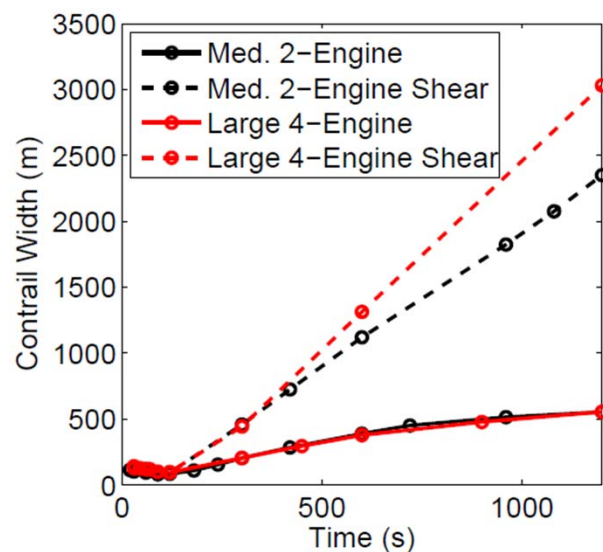
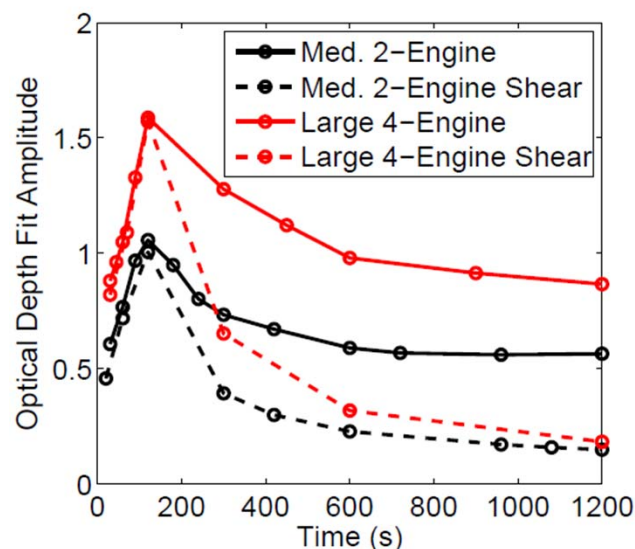
# Sensitivity Cases – Optical Properties



- Aircraft type cases
- Larger aircraft produced optically thicker contrails
  - Higher number density
  - Larger ice surface area
  - Both due to more emitted nuclei
- Larger aircraft initially produced wider contrails
  - Width at early times controlled by wingspan
  - Width at late times controlled by turbulence
  - Long term effect of aircraft size uncertain based on 20-minute results



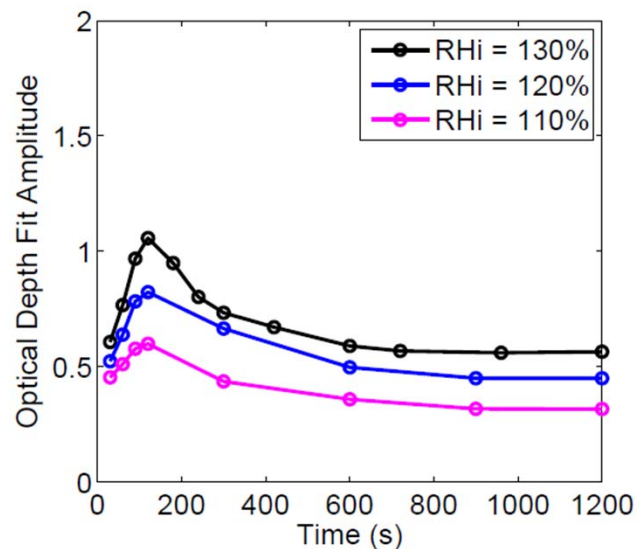
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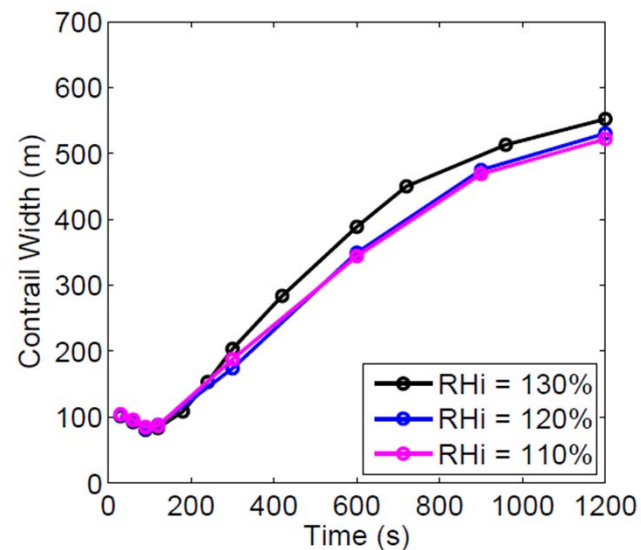
- Vertical shear cases
- Optical depth and contrail width unaffected by shear during vortex phase
- Both properties controlled by shear during dispersion phase
  - Kinematic effect of shear produces thin, wide clouds



# Sensitivity Cases – Optical Properties

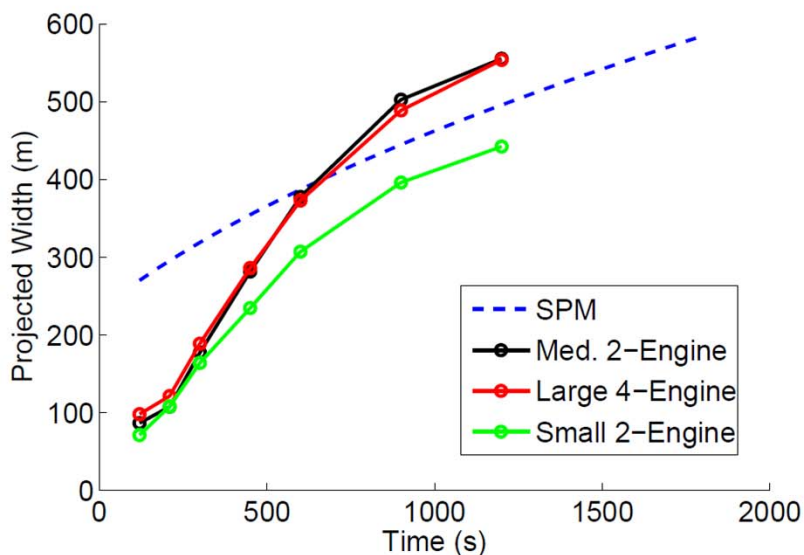
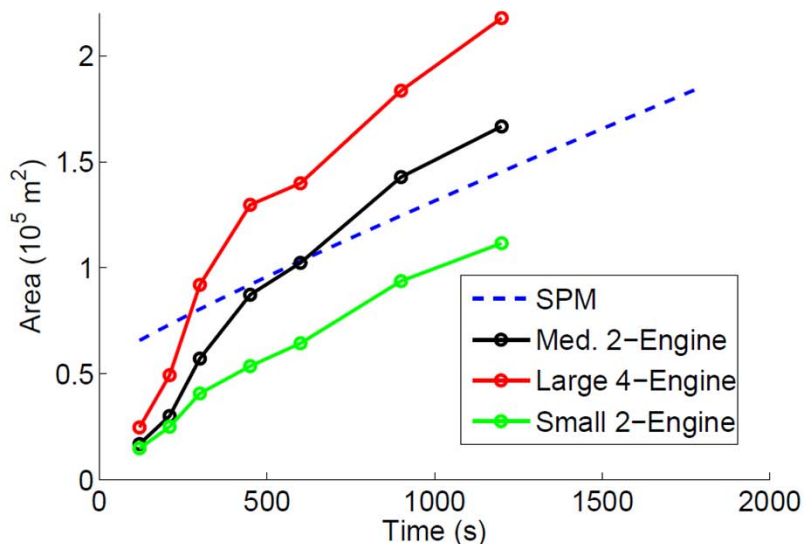


- Ambient relative humidity cases
- Higher humidity produced optically thicker contrails
  - Larger ice surface area due to larger particle sizes



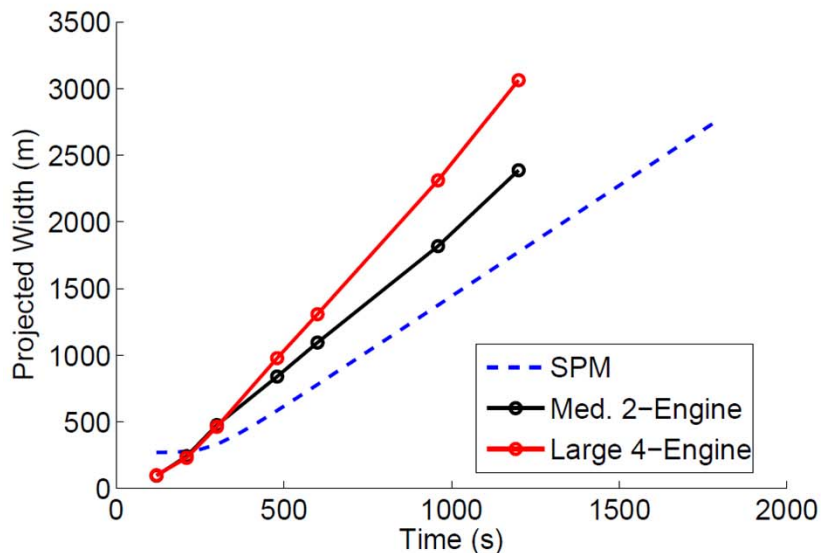
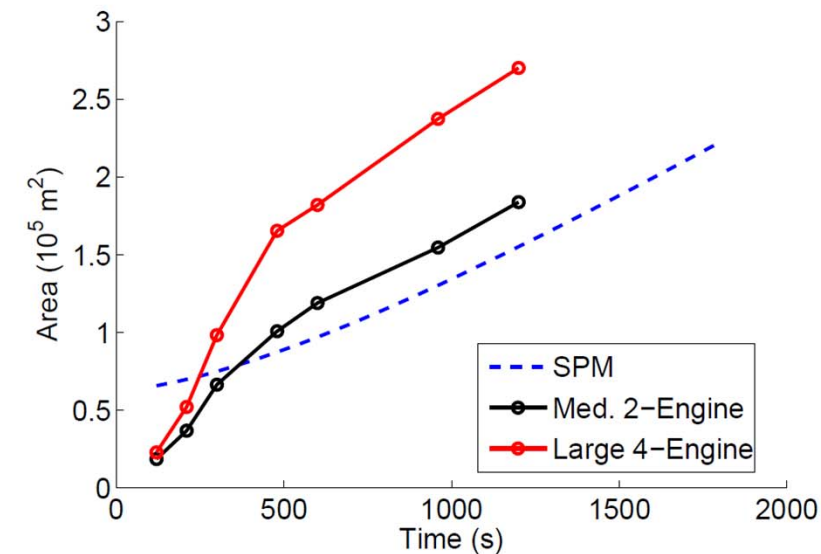
- Negligible effect on contrail width

# Parameterized Model – LES Data Comparison



- SPM is the basic parameterized model described in *Naiman, et al. 2010*
- Basic SPM initial condition set to match zero shear, medium aircraft result at  $t = 10$  minutes
- Appears to capture growth rate of area and width, but longer time LES needed for meaningful comparison
- Does not account for variations in initial condition with aircraft type

# Parameterized Model – LES Data Comparison



- Basic SPM initial condition set to match zero shear, medium aircraft result at  $t = 10$  minutes
- Similar to comparison with zero shear cases
  - Appears to capture growth rate of area and width, but longer time LES needed for meaningful comparison
  - Does not account for variations in initial condition with aircraft type

# Conclusions

- LES:
  - Optical properties relevant to climate impact strongly sensitive to vertical shear – mostly due to kinematic effect
  - Sensitivity in optical depth to aircraft type and ambient humidity
  - Long term sensitivity in width to aircraft type uncertain
- Parameterized model:
  - Captures growth rates of contrails
  - Lacks sensitivity to aircraft type
  - Longer time LES needed for comparison



# Future Work

- LES:
  - Incorporate ice habit parameterization to more realistically model ice crystal growth
  - Implement turbulence forcing for longer time horizon simulations (2-3 hours)
- Improve SPM for global climate modeling
  - Initial condition can be varied with aircraft type based on vortex wake descent parameters
  - Wake descent speed =  $\Gamma / (2 \pi b)$
  - Descent time characterized by vortex system lifetime based on turbulence intensity (*Crow and Bate, 1976*)



# Acknowledgements

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# Additional Slides



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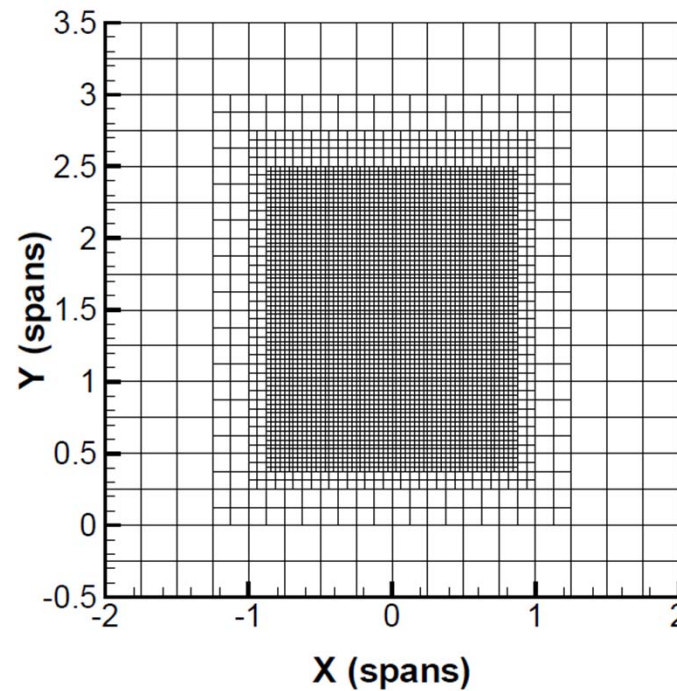
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# Case Summary

Sensitivity	Initial Condition	Wind Shear	RHi	$EI_{ice}$	$N_{bv}$
A/C Type	Medium 2-Engine	0	130%	$10^{15}$	$0.01 \text{ s}^{-1}$
A/C Type	Large 4-Engine	0	130%	$10^{15}$	$0.01 \text{ s}^{-1}$
A/C Type	Small 2-Engine	0	130%	$10^{15}$	$0.01 \text{ s}^{-1}$
Shear	Medium 2-Engine	$0.005 \text{ s}^{-1}$	130%	$10^{15}$	$0.01 \text{ s}^{-1}$
Shear	Large 4-Engine	$0.005 \text{ s}^{-1}$	130%	$10^{15}$	$0.01 \text{ s}^{-1}$
RHi	Medium 2-Engine	0	120%	$10^{15}$	$0.01 \text{ s}^{-1}$
RHi	Medium 2-Engine	0	110%	$10^{15}$	$0.01 \text{ s}^{-1}$
$EI_{ice}$	Medium 2-Engine	0	130%	$10^{14}$	$0.01 \text{ s}^{-1}$
$EI_{ice}$	Medium 2-Engine	0	110%	$10^{14}$	$0.01 \text{ s}^{-1}$
Stability	Medium 2-Engine	0	130%	$10^{15}$	0
Stability	Medium 2-Engine	0	130%	$10^{15}$	$0.015 \text{ s}^{-1}$

# Grid Example

	Stage 1	Stage 2	Stage 3	Stage 4	Stage 5	Stage 6	
Simulation Time	0-30	30-60	60-120	120-300	300-600	600-1200	s
Domain Size	8x8x8	8x8x8	8x8x8	16x16x8	24x24x8	32x32x8	$b^3$
Central Resolution	1/128	1/64	1/64	1/32	1/24	1/16	b
Number of Nodes	$34 \times 10^6$	$18 \times 10^6$	$33 \times 10^6$	$20 \times 10^6$	$17 \times 10^6$	$14 \times 10^6$	



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Contrails over Stanford, CA, 3 October 2009